Universal Properties of Mythological Networks

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PACS 89.75.-k - Complex systems
PACS 89.75.Hc - Networks and genealogical trees
PACS 89.65.Ef - Social organizations; anthropology

Abstract - As in statistical physics, the concept of a itative, role in the field of comparative mythology. He analyse the networks underlying three iconic mythologomous and distinguishing quantitative features. Of Greek text are mostly believed by antiquarians to be Irish epic, is often considered to be fictional. Here we criminate real from imaginary social networks and play between them. This suggests that the perceived article back to anomalous features associated with six chara of several entities or proxies, renders the plausibility from a network-theoretic point of view.

Introduction. - Over the past decades many statistical physicists have turned their attention to other disciplines in attempts to understand how properties of complex systems emerge from the interactions between component parts in a non-trivial manner. Applications includes Abstract -As in statistical physics, the concept of universality plays an important, albeit qualitative, role in the field of comparative mythology. Here we apply statistical mechanical tools to analyse the networks underlying three iconic mythological narratives with a view to identifying common and distinguishing quantitative features. Of the three narratives, an Anglo-Saxon and a Greek text are mostly believed by antiquarians to be partly historically based while the third, an Irish epic, is often considered to be fictional. Here we use network analysis in an attempt to discriminate real from imaginary social networks and place mythological narratives on the spectrum between them. This suggests that the perceived artificiality of the Irish narrative can be traced back to anomalous features associated with six characters. Speculating that these are amalgams of several entities or proxies, renders the plausibility of the Irish text comparable to the others

plex systems emerge from the interactions between component parts in a non-trivial manner. Applications include the analysis of complex networks in the natural, social and technological sciences as well as in the humanities [1–5]. One of the notions intrinsic to statistical physics is universality, and attempts have been made to classify complex networks from a variety of areas to facilitate comparison amongst them [6,7].

Universality is also an important, albeit hitherto qualitative, notion in the field of comparative mythology. Campbell maintained that mythological narratives from a variety of cultures essentially share the same fundamental structure, called the monomyth [8]. Here we statistically compare networks underlying mythological narratives from three different cultures to each other as well as to real, imaginary and random networks. In this way we quantitatively explore universality in mythology and attempt to place mythological narratives on the spectrum from the real to the imaginary.

Network theory has recently been developed and applied to polymers, economics, particle physics, computer science, sociology, biology, epidemiology, linguistics and more [1-7,9-11]. A number of statistics have been developed to capture features of such networks. Some structural properties are quantified using the characteristic path length ℓ , the longest geodesic $\ell_{\rm max}$ and the clustering coefficient C. The first of these is a measure of the average minimum separation between pairs of N nodes and ℓ_{max} is the diameter of the network. Clustering measures to what extent a given neighbourhood of the network is cliqued. If node i has k_i neighbours, then the maximal number of potential edges between them is $k_i(k_i-1)/2$. If n_i is the actual number of bonds between the k_i neighbours of i, the clustering coefficient of the node is [9]

$$C_i = \frac{2n_i}{k_i(k_i - 1)}. (1)$$

Many complex networks have a modular structure implying that groups of nodes organise in a hierarchical manner into increasingly larger groups. Hierarchical networks are characterised by a power-law dependency of the clustering coefficient on the node degree [12–14],

$$C(k) \sim \frac{1}{k}. (2)$$

The mean degree $\langle k \rangle$ is obtained by averaging over the nodes of the network and its clustering coefficient C is obtained by averaging eq.(1). A network is said to be small world if $\ell \approx \ell_{\rm rand}$ and $C \gg C_{\rm rand}$, where $\ell_{\rm rand}$ is the average path length and $C_{\rm rand}$ is the clustering coefficient of a random network of the same size and average degree [9].

Network		N	$\langle k \rangle$	ℓ	ℓ_{rand}	$\ell_{\rm max}$	C	$C_{\rm rand}$	G_c	r
Beowulf	All	74	4.45	2.37	2.88	6	0.69	0.06	50 (67.5%)	-0.10
	Hostile	31	1.67	2.08	3.25	4	0	0.05	10 (32.2%)	-0.20
	Friendly	68	4.12	2.45	2.98	6	0.69	0.06	45~(66.1%)	-0.03
Táin	All	404	6.10	2.76	3.32	7	0.82	0.02	398 (98.5%)	-0.33
	Hostile	144	2.33	2.93	5.88	7	0.17	0.02	131 (90.9%)	-0.36
	Friendly	385	5.67	2.84	3.43	7	0.84	0.01	350~(90.9%)	-0.32
Iliad	All	716	7.40	3.54	3.28	11	0.57	0.01	707 (98.7%)	-0.08
	Hostile	321	2.25	4.10	7.12	9	0	0.01	288 (89.4%)	-0.39
	Friendly	664	6.98	3.83	3.34	12	0.62	0.01	547 (82.3%)	0.10
Beowulf*	Friendly	67	3.49	2.83	3.36	7	0.68	0.05	43 (64.2%)	0.01
Táin*	Friendly	324	3.71	3.88	4.41	8	0.69	0.01	201 (62.0%)	0.04

Table 1: Size, mean degree, mean path length, diameter, clustering coefficient, absolute (relative) size of giant component and assortativity r for the epics, together with mean path length $\ell_{\rm rand}$ and clustering $C_{\rm rand}$ for similarly sized random networks.

If p(k) is the probability that a given vertex has degree k, then the degree distribution for many networks is

$$p(k) \sim k^{-\gamma},$$
 (3)

for positive constant γ , with perhaps a cut-off for high degree. Such power laws indicate that, while most nodes are sparsely connected, some are linked to many others and play an especially important role in maintaining network integrity. Networks are scale free if the power law (3) holds with $2 < \gamma \le 3$ [6]. Assortative mixing by degree is the notion that vertices of high degree associate with similarly highly connected vertices, while vertices of low degree associate with other less linked nodes.

Another measure of the connectivity of the network is the size of the giant component G_c . In a scale-free network, removal of influential nodes causes the giant component to break down quickly whereas it remains intact upon randomly removing nodes from the network [15]. As well as the degree, the betweenness centrality of a node g_l indicates how influential that node is, it controls the flow of information between other vertices. It is the total number of geodesics (shortest paths) that pass through a given node [16]. If $\sigma(i,j)$ is the number of geodesics between nodes i and j, and if the number of these which pass through node l is $\sigma_l(i,j)$, the betweenness centrality of vertex l is

$$g_l = \frac{2}{(N-1)(N-2)} \sum_{i \neq j} \frac{\sigma_l(i,j)}{\sigma(i,j)}.$$
 (4)

The normalization ensures that $g_l = 1$ if all geodesics pass through l.

The above statistics capture a variety of characteristics of networks and, by comparing them between different networks, we get an idea how similar or different they are. These quantitative indicators therefore play similar roles to critical exponents in the study of phase transitions.

Social networks are usually small world [6, 9], highly clustered, assortatively mixed by degree [17, 18] and scale free [6,19]. Some real social networks that have been studied include between company directors [20], jazz musicians

[21], movie actors [6,9], scientific co-authors [22–25] as well as online social networks [26–28]. Catalogues of the properties of these and other networks are contained in, e.g., refs. [2, 3]. In refs. [14, 29] the social network of characters appearing in Marvel comics (the so-called Marvel Universe) was constructed. In that network two characters are connected if they appear in the same comic book. This is clearly an artificial social network as the characters in this universe represent an imaginary society, but it is a social network nonetheless. Analysis showed that, while it mimicked other social networks to an extent, it was unable to hide its artificial nature [14, 29]. To facilitate comparison between our mythological networks and other real and imaginary networks, we also look here at four works of fiction. With these at our disposal, we seek to compare mythological narratives to other networks, ranging from the real to the imaginary.

Comparative mythology. – The mythological narratives studied here are Beowulf [30], the Iliad [31] and the Táin Bó Cuailnge [32]. In comparative mythology, these have statuses similar to that of the Ising model in statistical physics. They are widely studied, frequently compared to each other and still present puzzles which continue to be investigated. Beowulf is an Old English heroic epic, set in Scandinavia. A single codex survives which is dated from between the 8th and early 11th centuries [33, 34]. Although the poem is embellished by obvious fiction, archaeological excavations in Denmark and Sweden support historicity associated with some of the human characters although the main character Beowulf is mostly not believed to have existed [35,36]. The *Iliad* is an epic poem attributed to Homer and is dated to the 8th century BC [31]. Recent evidence suggests that the story may be based on a historical conflict during the 12th century BC [37,38]. The Táin Bó Cuailnge ("Táin" from here on) is an Irish epic, surviving in three 12th and 14th century manuscripts. It describes a conflict between Connaught and Ulster, Ireland's western and northern provinces. Before it was committed to writing, the Táin had an extensive oral history. It was dated by medieval scholars to the first centuries BC, but this may have been an attempt by Christian monks to artificially synchronise oral traditions with biblical and classical history [32]. Its historicity is often questioned. Jackson (1964) argues that such narratives corroborate Greek and Roman accounts of the Celts and offer us a 'window on the iron age' [39] but O'Rahilly (1964) objects that such tales have no historical basis whatsoever [40].

From the databases created for each mythological epic, 74 unique characters were identified in Beowulf, 404 for the Táin and 716 for the Iliad. (The reader should keep in mind that these networks, like many others [2], are necessarily of limited extent and incomplete - potentially representing spotlights on the societies from which they are drawn.) We define two distinct relationship types: friendly and hostile edges. Friendly links are made if two characters are related; speak directly to one another; speak about one another or are present together and it is clear they know each other. Hostile links are made when two characters meet in a conflict and a friendly link is not made if they speak here and only here; or when a character explicitly declares animosity against another and it is clear they know each other. To ensure consistency throughout, we first separately constructed the network for one of the narratives. Comparing our individual interpretations allowed us to tune the rules to a consistent and implementable set and to satisfy ourselves that the networks could be constructed in a reasonably objective manner. We also inspected different translations of the original texts to verify that these did not result in significant differences to our quantitative results.

In table 1 a list of statistics for the networks underlying each epic is compiled. These include the mean degree $\langle k \rangle$, the average path length ℓ , diameter $\ell_{\rm max}$, clustering coefficient C, the size of the giant component G_c in absolute terms and as a percentage of the size N, and the assortativity r. In addition the average path length $\ell_{\rm rand}$ and the clustering coefficient $C_{\rm rand}$ for a random network of the same size and average degree are listed. The statistics indicate that the complete networks are similar to the friendly ones reflecting that, even though conflict is an element of each narrative, they are still stories about human relations, and the discussions rather than disputes drive the stories. Like real social networks the mythological networks have average path lengths similar to those of random networks of the same size and average degree. They also have high clustering coefficients compared to random networks indicating they are small world. The hostile networks are quite different; the facts that their average path lengths are smaller than those of random networks and that they have virtually no clustering tell us they are not small world. The reason for such low clustering in hostile networks relates to the idea of 'the enemy of my enemy is my friend' – in general a common foe tends to suppress hostilities between two nodes.

In the overall network, closed triads with just one hostile

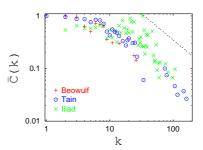


Fig. 1: Mean clustering coefficient per degree $\bar{C}(k)$ vs k for the three myths with the power law 1/k as a dashed line to guide the eye.

edge are also disfavoured as a single hostile link prompts the opposite node in a triangle to take sides. The propensity to disfavour odd numbers of hostile links in a closed triad is known as structural balance [41, 42]. Structural balance has been observed in real-world situations, such as the shifting alliances in the lead-up to war [43]. We find similar results in our three networks with only 3.8% of Beowulf's closed triads containing an odd number of hostile links, 8.0% of the Táin's and just 1.7% of the Iliad's.

In fig. 1 we test for hierarchical structure by plotting the mean clustering coefficient per degree $\bar{C}(k)$ versus k and comparing with eq.(2). The nodes with a smaller degree present higher clustering than those with larger degree and the decay approximately follows eq.(2). The nodes with low degree are part of densely interlinked clusters, while the vertices with high degree bring together the many small communities of clusters into a single, integrated network.

In most collaboration networks, a very large subset of nodes are connected to each other (the giant component). The full Táin and Iliad networks contain about 98% of the nodes. Beowulf has a smaller giant component (68% of all nodes) because the narrative contains two stories dealing with events from the past, disconnected from the main plot. Usually for collaboration networks, the giant components contain less than 90% of all nodes [23] and the friendly networks of each epic falls into this category. Removing the top 5% of nodes with the highest betweenness centrality causes all three networks to break down quickly, reducing the giant component of Beowulf and the Táin by over 30%. This lack of robustness shows how reliant they are on the most connected characters. If, however, 5% of the nodes are removed at random the giant component in each case is largely unaffected. Vulnerability to targeted attack but robustness to random attack, and the hierarchical structure of the networks, hint that these networks may be scale free.

Newman showed that real social networks tend to be assortatively mixed by degree [17] and Gleiser demonstrated that disassortativity of social networks may signal artificiality [14]. However disassortivity may also reflect the

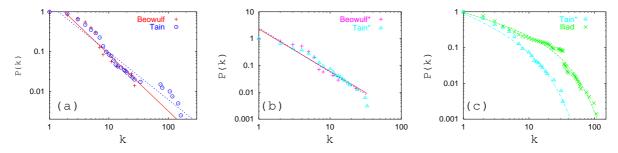


Fig. 2: The degree distribution (a) as a power law for Beowulf and the $T\'{a}in$ (b) for $Beowulf^*$ and the $T\'{a}in^*$ and (c) as truncated power laws for the $T\'{a}in^*$ and the Iliad.

conflictual nature of the stories. In the *Táin* and the *Iliad*, in particular, characters are frequently introduced to fight one of the heroes and are killed virtually immediately. These encounters link the high-degree heroes to low-degree victims and may explain why the hostile networks are highly disassortative. This suggests that only in the friendly networks may disassortativity be confidently interpreted as signaling artificiality.

The assortativity coefficient r is given by the Pearson correlation coefficient of the degrees between all pairs of linked nodes and is listed for each network in table 1. Positive correlation indicates assortative mixing and a negative value indicates disassortativity. As expected, all hostile networks are strongly disassortative. However, the *Iliad* friendly network is assortative and the *Beowulf* friendly network is only mildly disassortative. Beowulf takes place in two different settings, years apart, with the eponymous protagonist being the only character to appear in both places. As it is a small network, the main character has high degree but most of his neighbours have lower degree rendering the network disassortative. Indeed, removing the protagonist (labeling the resulting network *Beowulf**) delivers a positive assortativity coefficient (r = 0.012) for the interactions between the remaining characters.

Thus the Iliad and $\mathit{Beowulf}^*$ friendly networks have properties associated with real social networks. While the $\mathit{T\'{a}in}$ has many such features, it is not assortative. This corroborates antiquarians' interpretations of the historicity of these myths (obviously fabulous entities and interactions notwithstanding) – the societies in the Iliad and $\mathit{Beowulf}^*$ (without the eponymous protagonist) may be based on reality while that of the $\mathit{T\'{a}in}$ appears fictional [40]. We next turn our attention to networks which are definitely fictional, before an analysis of degree distributions which will illuminate the reasons behind the apparent artificiality exhibited by the $\mathit{T\'{a}in}$.

Fictional Narratives. — The above characteristics of the three mythological networks distinguish them from the intentionally fictitious Marvel universe studied in refs. [14,29]. The question arises whether these characteristics are properties of non-comic fictional literature in general or whether this may truly signal a degree of historicity

underlying the three mythological narratives. To investigate this, we applied our network tools to four narratives from fictional literature. These are Hugo's Les Misérables (N=77), Shakespeare's Richard III (N=70), Tolkien's Fellowship of the Ring (the first part of the Lord of the Rings trilogy, with N=118) and Rowling's Harry Potter (N=72). We found that each of these, together with the Marvel universe $(N=6\,846)$, has a very high clustering coefficient, is disassortative and has a giant component containing almost every character.

Attacking the smaller fictional networks by removing the top five characters with the highest betweenness centralities, we find that the networks are quite robust. The giant component goes from 100% to 73.6% for Les Misérables, 94.3% to 84.6% for Richard III, 94.1% to 85.8% for Fellowship of the Ring and 97.2% to 77.4% for Harry Potter. Removing the top 10% of nodes with highest betweenness shows Les Misérables and Harry Potter are less robust than the others, however the Marvel Universe is barely affected by losing the top 684 vertices. This robustness is also indicative of an exponential degree distribution (see below and ref. [15]). The robustness and the high clustering coefficient shows how well connected the networks are. All five fictional networks have a hierarchical structure. While these networks display the high clustering coefficient that is common to all social networks, the fact that they are all disassortative and are almost entirely connected is perhaps an indication of their societies' artificiality. In a sense they are too small world to be real.

Degree distributions. — We finally turn to the degree distributions associated with the various networks. This will allow us to identify the source of the disassortativity of the *Táin* in particular and to speculate as to what it would take to render that network more realistic.

The cumulative distribution functions for the three narratives are plotted in fig. 2. Estimates from eq.(3) for Beowulf, the Táin and the Iliad yield $\gamma = 2.4 \pm 0.2, 2.2 \pm 0.1$ and 2.4 ± 0.1 (with χ^2/df 0.3, 0.2 and 0.4), respectively. The degree exponents for the friendly networks are very similar to these values. These results signal that the degree distributions of these networks are indeed scale free.

For comparison, the degree distribution for the fictional

narratives only follows a power law in the tail in one instance (*Harry Potter*) and only this appears to be scale free. The other three, as the Marvel Universe, are better described by exponential distributions.

In fig. 2(a) we observe a striking similarity between the degree distributions of Beowulf and the Táin for all but the six most connected characters in the latter. In fact, omitting the corresponding 6 points delivers the estimate $\gamma = 2.4 \pm 0.1$, the same value as for Beowulf and the Iliad. However, we have no legitimate basis to omit the six most important characters of the narrative, especially if the degree distribution is scale free, because our previous results indicate this would destroy the giant component. Instead we speculate that these six characters are in fact amalgams of several entities or proxies, whose collective degrees are large, but whose individual degrees are reduced. To test this hypothesis, we removed the weak links (where they interact with characters only once in the entire narrative) from the characters and denote the result by Táin*. In fig. 2(b), this is compared to Beowulf* as a power law. Because six characters now have lower degree, the estimate for γ increases. The modified exponent is $\gamma = 2.65 \pm 0.10$ ($\chi^2/\mathrm{df} = 0.15$), close to for Beowulf*, which has $\gamma = 2.58 \pm 0.19$ ($\chi^2/df = 0.27$). The steeper slope, particularly for large k, is indicative of the presence of a fast decay and is common in many networks. To understand this a comparison of the Táin with the larger network of the *Iliad* is appropriate.

The Iliad is, in fact, better fitted by a truncated power law $P(k) \sim k^{1-\tau} \exp{(-k/k^*)}$ with $\tau = 1.51 \pm 0.03$ ($\chi^2/\mathrm{df} = 0.07$). The $\mathit{Táin}^*$ is compared to Iliad in fig. 2(c). It is also well fitted by a truncated power law and delivers $\tau = 1.74 \pm 0.06$ ($\chi^2/\mathrm{df} = 0.03$).

The modified friendly $T \dot{a} in^*$ network has assortativity coefficient r=0.042. This positive value, together with the fact that the fitted degree distribution captures the top six data, ensures that the networks share all the properties of real social networks. (In comparison, simply removing the top six characters results in r=-0.122 and destroys the giant component.)

Another way to test for assortativity is to plot the degree of the neighbours of a vertex as a function of its degree. Positive slope indicates assortativity and negative slope signals disassortativity. Plots for the averages of the neighbouring degrees are contained in fig. 3. Beowulf and the Iliad are assortative, while the $\mathit{Táin}$ is clearly disassortative. However, removing weak links associated with the six strongest characters (resulting in the $\mathit{Táin}^*$ network) again renders that Irish narrative assortative, suggesting possibly historicity on a level comparable to $\mathit{Beowulf}$.

Conclusions. — We have analysed the networks of relationships between characters of three mythological epics and four fictional narratives and compared them to each other and to other social networks, both real and imaginary. We found that all seven networks are small world, highly clustered, hierarchical and resilient to random at-

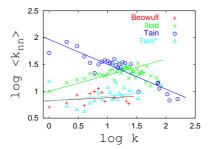


Fig. 3: The average $\langle k_{\rm nn} \rangle$ of the degrees of the neighbours of vertices of degree k and accompanying trend lines. Positive (negative) trends indicate assortativity (disassortativity).

tack – properties generally associated with real social networks. The fictional networks are, however, discernable from real social networks in that they mostly have exponential degree distributions, have relatively larger giant components, are robust under targeted attack and are dissassortative. Moreover, they share this latter set of properties with the network underlying the Marvel universe previously studied in refs. [14, 29].

In an attempt to place the three mythological networks on the spectrum from the real to the fictitious, we compared their properties to actual and imaginary social networks. Table 2 summarises the broad properties of the different types of networks. Of the three myths, the network of characters in the *Iliad* has properties most similar to those of real social networks. It has a power-law degree distribution (with an exponential cut-off), is small world, assortative, vulnerable to targeted attack and is structurally balanced. This similarity perhaps reflects the archaeological evidence supporting the historicity of some of the events of the *Iliad*.

There is also archaeological evidence suggesting some of the characters in *Beowulf* are based on real people, although the events in the story often contain elements of fantasy associated with the eponymous protagonist. The network for this society, while small, has some properties similar to real social networks, though like all the fictional narratives it is disassortative. However, removing the main character from the network renders it assortative. Thus, while the entire network is not credible as reflecting a real society, we suggest that an assortative subset has properties akin to real social networks, and this subset has corroborative evidence of historicity.

Currently there is very little evidence for the events and the society in the $T\acute{ain}$. While there is some circumstantial evidence in terms of the landscape [44], its historicity is often questioned [39,40]. Indeed, the social network of the full narrative initially seems similar to that of the Marvel Universe perhaps indicating it is the Iron Age equivalent of a comic book. However, comparing the $T\acute{ain}$'s degree distribution to that of Beowulf reveals a remarkable similarity, except for the top six vertices of the Irish narra-

Table 2: Summary of properties of mythological networks (Beowulf*, $T\acute{a}in^*$ and Iliad) compared to social and fictional networks. Here, small world implies $\ell \approx \ell_{\rm rand}$, $C \gg C_{\rm rand}$, hierarchical means that $C(k) \sim 1/k$ and scale free refers to a power-law degree distribution with $\gamma \leq 3$. "TA" and "RA" refer respectively to resilience to targeted and random attacks.

	Social	Myth (friendly)	Fiction
Small world	Yes	Yes	Yes
Hierarchy	Yes	Yes	Yes
p(k)	Power law	Power law	Exp.
Scale free	Yes	Yes	No
G_c	< 90%	< 90%	> 90%
TA	Vulnerable	Vulnerable	Robust
RA	Robust	Robust	Robust
Assortative	Yes	Yes	No

tive. This suggests the artificiality of the network may be mainly associated with the corresponding characters. They are similar to the superheroes of the Marvel Universe – too super-human to be realistic, or in terms of the network, they are too well connected. We speculate that these characters may in fact be based on amalgams of a number of entities and proxies. To test the plausibility of this hypothesis, we removed the weak social links associated with these six characters. The resulting network is is assortative, similar to the *Iliad* and to other real social networks and very different to that of the Marvel Universe and works of fiction. We therefore suggest that if the society in the *Táin* is to be believed, each of the top six characters is likely an amalgam that became fused as the narrative was passed down orally through the generations.

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The authors thank Christian von Ferber, Colm Connaughton and Martin Weigel for helpful comments and discussions, Heather O'Donoghue for help with the mythological epics, Aneesa Ayub, Rachel Findlay and Simon Rawlings for help with the data for the fictional narratives. This work is supported by The Leverhulme Trust under grant no. F/00 732/I.

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